

THEORY OF MACHINES

Question 1:

The sun gear 1, of the planetary gear train (shown in Fig.(1)), has 26 external gear teeth, the planet gear 2 has 22 external gear teeth, the planet gear 2' has 30 external gear teeth, the sun gear 4 has 20 external gear teeth, the planet gear 5 has 18 external gear teeth, and the ring gears 3, 6 are internally teathed.

The gears 2 and 2' are fixed on the same shaft. The gear 1 rotates with input angular speed 100 rpm, in clockwise (CW) direction, and the ring gear 3 is fixed (not rotate). All the gears have the same module.

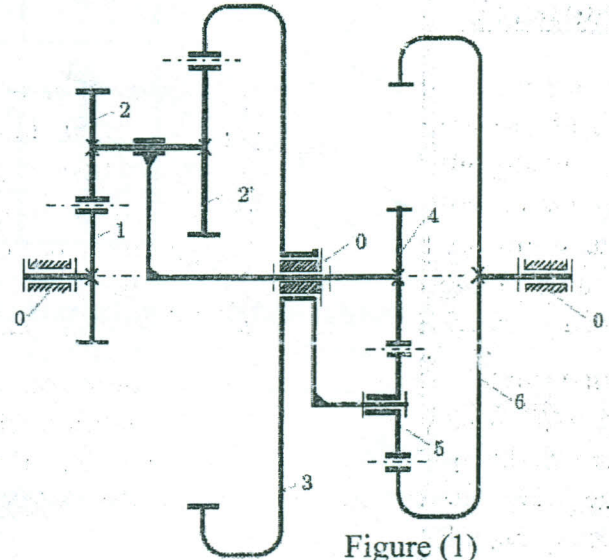


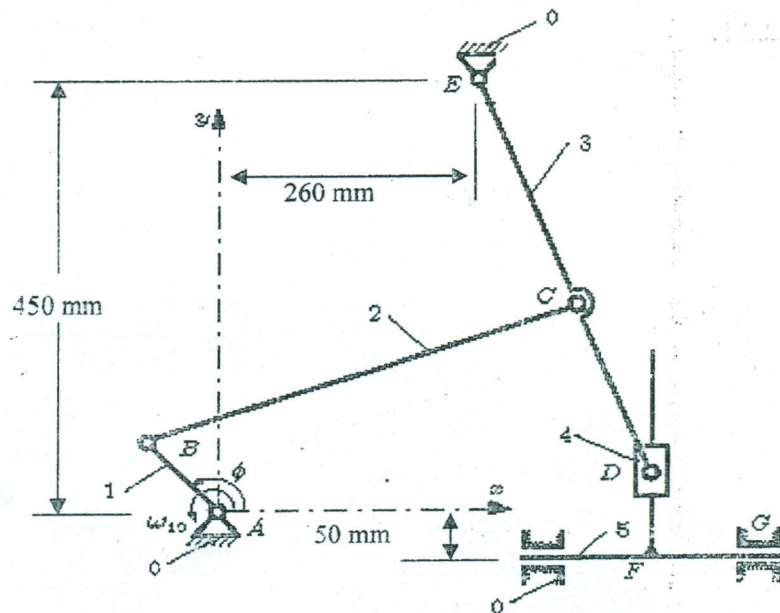
Figure (1)

Find:

- The number of teeth of the internally teathed ring gears 3, 6.
- The angular velocity and direction of rotation (CW or CCW) of each gear.

Question 2:

Figure (2)



For the mechanism shown in Fig. (2), the crank AB inclined by $\phi = 120^\circ$, and rotates with constant angular velocity ω_{10} equals 1 rad./sec (CCW). The lengths of differ at links are: $AB = 100$ mm, $BC = 450$ mm, $ED = 450$ mm, $EC = 250$ mm.

Find ;

- The magnitude and direction of velocity and acceleration of slider F, and
- The angular velocity and the angular acceleration of link DE.

Question 3:

Four masses *A*, *B*, *C* and *D*, given in table below are to be completely balanced. The planes containing masses *B* and *C* are 300 mm apart. The angle between planes containing masses *B* and *C* is 90°. *B* and *C* make angles of 120° and 210° respectively with *D* in the same sense.

| Mass | Weight (N) | Radius (mm) |
|------|------------|-------------|
| A | <i>W</i> | 180 |
| B | 30 | 240 |
| C | 50 | 120 |
| D | 40 | 150 |

Find:

- (a) the weight and the angular position of mass *A*;
- (b) the position of planes *A* and *D*.

Question 4:

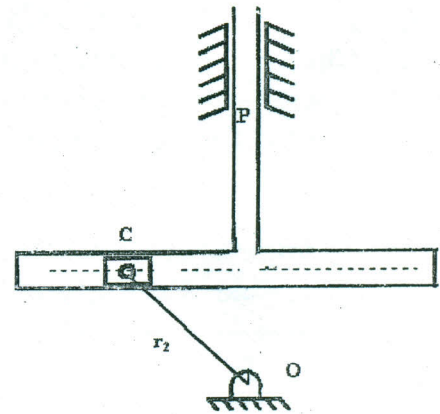
For the Scotch-yoke mechanism shown in Fig. 3

Given: $\theta_2 = 135^\circ$,

$\omega_2 = 1 \text{ rad/s}$ (in clockwise CW direction),

$\alpha_2 = 2 \text{ rad/s}^2$ (CCW direction), and the crank *OC* length, $(r_2) = 120 \text{ mm}$,

Find the velocity and acceleration of slider *P*.



Question 5:

Figure (4) shows a schematic diagram of an eight-link mechanism. The link lengths are ;

$AB = 450$ $OF = FC = 250$

$AC = 300$ $CG = 150$

$BD = 400$ $HG = 600$

$BE = 200$ $QH = 300$

Determine the required shaft torque on link 8 for static equilibrium against an applied load of 400 N on the link 3.

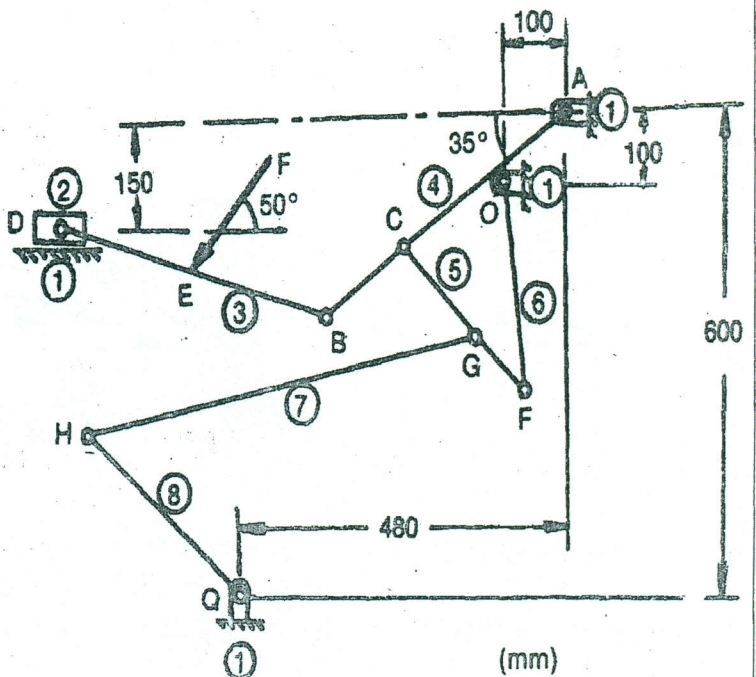


Figure (4)

With my Best Wishes for You &
Dr. SAMY EL-GAYYAR