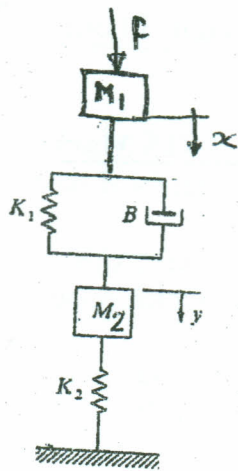
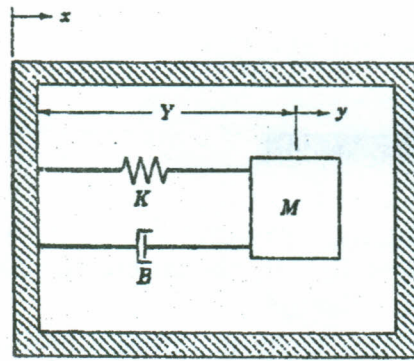


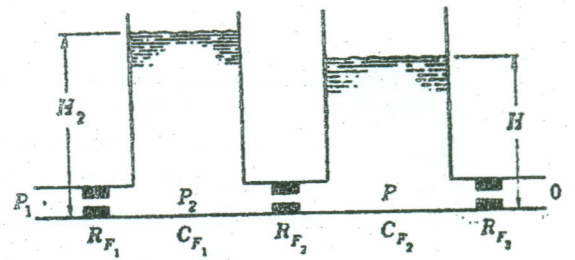
Problem (1)



(a)

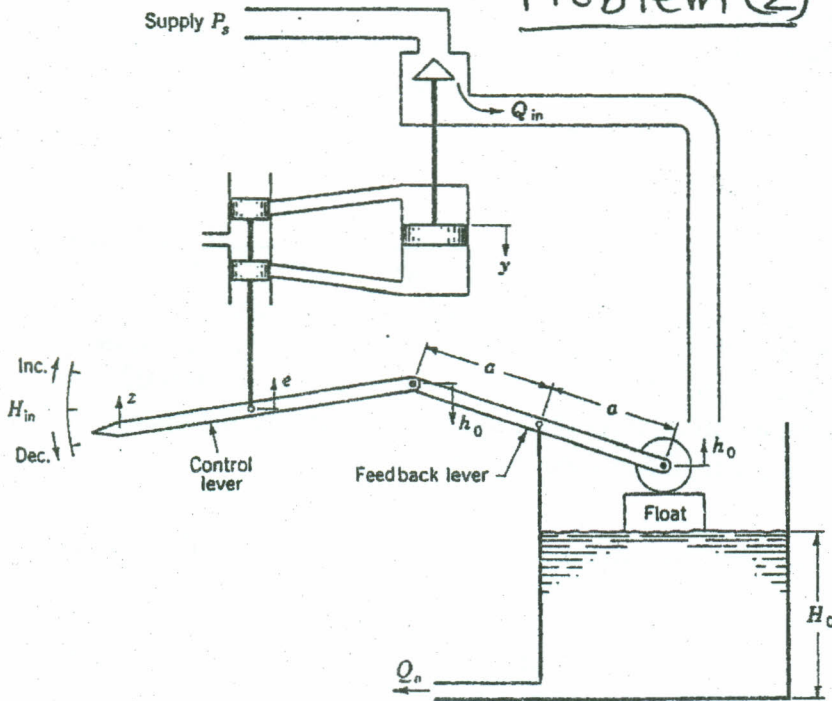


(b)

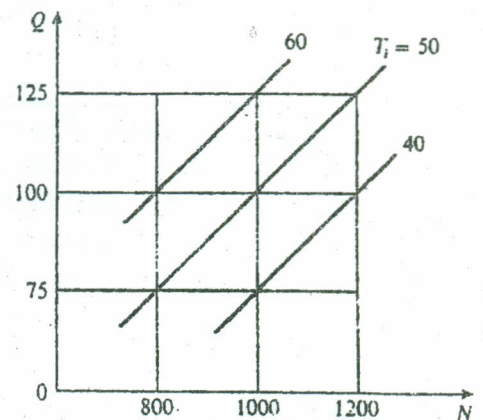


(c)

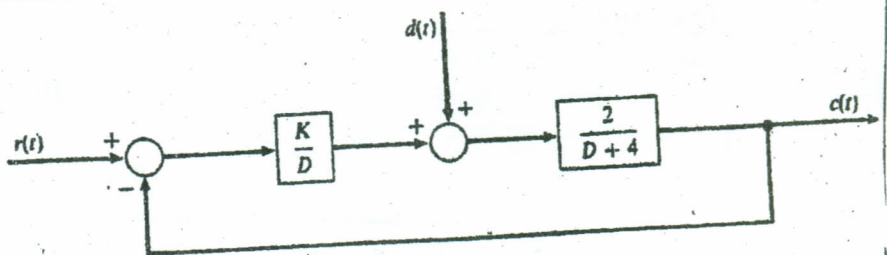
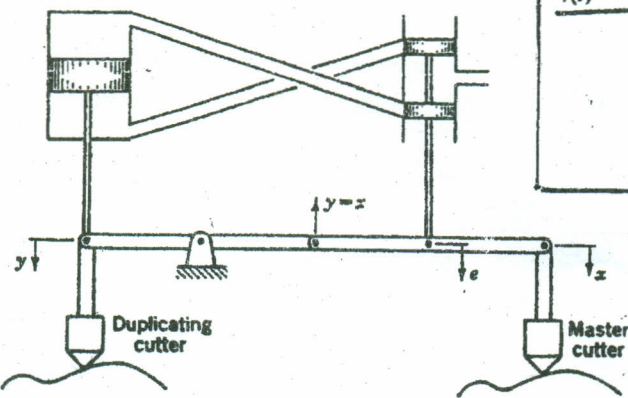
Problem (2)



Problem (3)



Problem (4)



Problem (5)

$f(t)$	$F(s)$	$f(t)$	$F(s)$
$\delta(t)$ <td>1</td> <td>t^n <td>$n!/s^{n+1}$</td> </td>	1	t^n <td>$n!/s^{n+1}$</td>	$n!/s^{n+1}$
$u(t)$ <td>$1/s$</td> <td>$t^n e^{at}$ <td>$n!/s^{n+1}$</td> </td>	$1/s$	$t^n e^{at}$ <td>$n!/s^{n+1}$</td>	$n!/s^{n+1}$
$t e^{at}$ <td>$1/s^2$</td> <td></td> <td></td>	$1/s^2$		
e^{at} <td>$1/(s-a)$</td> <td></td> <td></td>	$1/(s-a)$		

Attempt all questions

Question 1

(15 Mark)

a- For the mechanical systems shown write the force equation at each coordinate and then determine the equation which relates: (i) x to f (ii) y to f (iii) y to x .

b-A schematic diagram of an accelerator for measuring the linear acceleration d^2x/dt^2 is shown in figure. Determine the operational form for the differential equation which relates y to the acceleration D^2x of the frame.

c-The figure shows a fluid system of two tanks in series. Construct the fluid system representation for this system. Determine the equation of the pressure P ($H=P/\rho$) as a function of the inlet pressure P_1 (P_2 should not appear in the equation).

Question 2

(15 Mark)

The figure shows a liquid level controller. To raise the level of the fluid, the control lever is moved up (i.e. position z is raised). This raises the valve position $e=(z-h_0)/2$, which increases y , thereby admitting more flow Q_{in} . The flow Q_{in} is a function of the flow valve opening Y and the supply pressure P_s . The change in volume of liquid in the tank is the time integral $(q_{in}-q_0)/D$, which is equal to the cross sectional area of the tank AT times the change in level h_0 . The flow out Q_0 is seen to depend on the pressure head H_0 . Determine the overall block diagram for this system.

Question 3

(15 Mark)

The characteristics of an engine are described by the family of curves in Figure. Determine the linear approximation of the torque t delivered by the engine. The difference between the torque t produced by the engine and the load torque t_L is used to accelerate the engine $J dn/dt$ and to overcome viscous force $B n$. Thus, $t-t_L = J dn/dt + B n$. For $j=0.02$ and $B=0.03$, determine the differential equation relating the change in speed n to the change in fuel flow q and the change in load torque t_L . Determine the time constant τ .

Question 4

(15 Mark)

A reproducing shaper is shown in figure. The position y of the duplicating cutter is seen to follow the position x of the master cutter. Determine the mode of operation of the shaper. What modification would be necessary to convert this to a proportional plus integral controller?

Question 5

(15 Mark)

Robots can be programmed to move tool through path very accurately. For the robotic control system shown in figure, all the initial conditions are zero and $k=1.5$. Determine the response for the case when both $r(t)$ and $d(t)$ are unit step functions.

Question 6

(15 Mark)

Consider the differential equation $c(t) = \frac{12}{(D+1)(D+3)} r(t)$ Using classical methods, determine the solution when $f(t) = e^{-2t}$ for $y(0)=2$ and $y'(0)=0$